

Doctoral Course in:

Modelling Turbulent Dispersed Flows



Lesson Five:

Particles Entrainment, Deposition, Dispersion and Segregation

Lausanne, 11 June 2008



# A complicated scientific application...



Our motivation is turbulent dispersed and reactive flow modelling

1. Wednesday May 7: 14 pm to 17 pm

- **Introductory seminar.** Fundamentals on Stokes flow around a sphere.
- 2. Wednesday May 14: 14 pm to 17 pm
  - ☑ Forces acting on a sphere. Steady and transient forces
  - **☑** Heat and Mass transfer from a sphere.
  - ☑ Introduction to DNS of Turbulent Flow.
- 3. Wednesday May 21: 14 pm to 17 pm
  - ☑ Particles Interaction with Vortices;
  - ☑ Characterization of a Vortex;
  - **Vortex Dynamics in Boundary Layers**
  - **Particle dispersion in synthetic turbulence. Project description**
- 4. Wednesday May 28: 14 pm to 17 pm

Special topic on PDF approaches: Dr Abdel Dehbi, PSI.

5. Wednesday June 4: 14 pm to 17 pm

**NOT COVERED (JRT Course).** 

6. Wednesday June 11: 14 pm to 17 pm

Particle/Turbulence Interactions: Deposition & Entrainment in Boundary Layers. Are particles a compressible flow? Indicators for particles segregation Questions and Updates on the project

7. Wednesday June 18: 14 pm to 17 pm

Particle dispersion in synthetic turbulence. Project Advancement/Discussion

8. Wednesday June: 25:14 pm to 17 pm

**Project Discussion.** 

- 9. Wednesday July: 2: 14 pm to 17 pm
  - To be confirmed. Final Remarks



# Summary



#### What we know from previous lectures:

- **1** Forces acting on a sphere: We know EVERYTHING!
- 2 Unsteady and Turbulent Flows: We know something
- **3** Vortex Dynamics and Flow Structures in Boundary Layers and Shear Flows: We Know something

#### • What we will learn in today lecture:

- **1** Modelling/Simulation approaches (We will refresh some of the early concepts)
- 2 If we know the flow field at discrete points (Simulations), which fluid velocity will we use?
- **3** How Flow Structures in Boundary Layers control Deposition/Entrainment?
- 4 Measuring Particle Segregation/Dispersion
- 5 Updates on the Homeworks and Project
- 6 ??? Perhaps a Seminar on Bubbly Turbulent Flow (or next Wednesday)



<u>Refreshing the memory...</u> same concepts folded and unfolded differently...



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- 1. Modelling the dispersed phase >>(pointwise approximation);
- 2. Forces acting on particles;
- 3. 1Way/2Way/4Way coupling;
- 4. Interpolation methods.





One-way/Two-way/... coupling







### One-way/Two-way/... coupling



# <u>One-way coupling</u> (VF < 10<sup>-6</sup>; IS > 100): (Particle Momentum Balance)

Particles do not influence significantly the flow field  $\rightarrow$  Allows to investigate the effect of flow structure on particle motion/dispersion/distribution;

#### <u>Two-way coupling</u> (10<sup>-6</sup><VF<10<sup>-4</sup>; 10<IS<100) (Particle Momentum Balance; Fluid Momentum Balance)

Particles influence the flow field dynamics  $\rightarrow$  allows investigation of flow modulation by particles.

<u>More complex coupling</u> (10<sup>-3</sup><VF<10<sup>0</sup>; 1<IS<10) (Particle Momentum Balance; Fluid Momentum Balance; Fluid Mass Balance)

Particles influence the flow field dynamics  $\rightarrow$  allows investigation of flow modulation by particles.





# **TWO-WAY EFFECT** (point-force approximation) Fluid equations Drag force on particle $\nabla \cdot \mathbf{v} = 0$ $\left(\mathbf{f}_{fl}\right)_p = \frac{(\mathbf{v} - \mathbf{v}_p)}{\tau_p} f(Re_p)$ $\rho \frac{\partial \mathbf{v}}{\partial \rho} + \rho \mathbf{v} \cdot \nabla \mathbf{v} = \mu \nabla^2 \mathbf{v} - \nabla p + \tilde{\mathbf{f}}_{2w}$ - particle velocity $(f_{f_1})_{p_1}$ - fluid velocity (one-way) fluid velocity (two-way) Particle tracking $m_p \frac{\partial \mathbf{v}_p}{\partial \theta} = \left(\mathbf{f}_{fl}\right)_p$ $\frac{\partial \mathbf{x}_p}{\partial \theta} = \mathbf{v}_p$ Momentum exchange term $\tilde{\mathbf{f}}_{2w} = -\sum \left(\mathbf{f}_{fl}\right)_p \,\delta\left(\mathbf{x} - \mathbf{x}_p\right)$





Two-way coupling: PSI-CELL model (Crowe et al., 1977)

According to PSI-CELL (Particle-Source-In Cell) model for fluid-patricle coupling: fluid sees the particle as momentum and energy source;

total force exerted by each particle on the fluid is a body force distributed over faces or vertices of the cell containing the particle;

such force acts as a disturbance force on fluid flow and pressure field:

Vtwo-way=Vone-way+Vdisturbance; ptwo-way=pone-

way + pdisturbance



### Two-way coupling: PSI-CELL model (Crowe et al., 1977)



(A) Particle in the turbulent flow



(D) Overall force acting on the particle



#### PSI-CELL model



#### Navier-Stokes Equation including particle body force:

$$\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} = -\frac{\nabla p}{\rho} + \nu \nabla^2 \mathbf{v} + \mathbf{s}_p$$

#### **Particle-source Term:**

$$\mathbf{s}_{p} = -\sum_{n=1}^{N_{p}} \left[ -\frac{\nabla p_{n}^{\text{two-way}}}{\rho} + \nu \nabla^{2} \mathbf{v}_{n}^{\text{two-way}} \right]$$

where  $N_p$ =Overall Particle Number.

.B. PSI-CELL model neglects particle-particle interactions!





1

#### Drag Force acting on a Particle



• Drag force:

$$\mathbf{F}_{D} = \frac{1}{2} C_{D} \rho \frac{\pi D_{p}^{2}}{4} (\mathbf{v} - \mathbf{v}_{p}) | \mathbf{v} - \mathbf{v}_{p}$$

$$\begin{cases} C_D = \frac{24}{\text{Re}_p} \left[ 1 + 0.15 \,\text{Re}_p^{0.687} \right] \\ \text{Re}_p = \frac{\rho |v - v_p| d}{\mu} \end{cases}$$

 $C_d = f(Re_p)!$ 

**Drag coefficient** 

#### Particle Reynolds Num.





Lift Force acting on a Particle



**Lift force:** 
$$\mathbf{F}_{lift} = C_L m_f (\mathbf{v} - \mathbf{v}_p) \times \boldsymbol{\omega}$$





# Sign of the lift force







#### Other Forces Acting on a Particle



#### Gravity & buoyancy:

$$\mathbf{F}_{grav} = \left(m_p - m_F\right)\mathbf{g}$$

#### Pressure gradient:

$$\mathbf{F}_{prgr} = m_F \frac{D\mathbf{v}}{Dt}$$

#### Added mass term:

$$\mathbf{F}_{addm} = -m_F \frac{1}{2} \left( \frac{d\mathbf{v}_p}{dt} - \frac{D\mathbf{v}}{Dt} \right)$$

#### Basset (*hystory*) term:

$$\mathbf{F}_{Bass} = -\frac{3}{2}\pi d_p^2 \mu \int_{-\infty}^t \left(\frac{d\mathbf{v}_p}{d\tau} - \frac{d\mathbf{v}}{d\tau}\right) \frac{d\tau}{\left[\pi v \left(t - \tau\right)\right]^{1/2}}$$





#### Importance of the Forces



 $F_{drag} \rightarrow O(St^{-1})$ 

 $F_{prgr} \rightarrow O\left(\frac{\rho_f}{\rho_p}\right)$ 

# For heavy particles: only drag and gravity

 $F_{addm} \rightarrow O\left(\frac{\rho_f}{\rho_p}\right)$ 

 $F_{Bass} \rightarrow O\left(\left(\frac{\rho_f}{\rho_p}\right)^{1/2}\right)$ 

$$F_{lift} \rightarrow O\left(d_p^2 \frac{\sqrt{dv / dy}}{v}\right)$$



# Bibliography



Chung J.N., Troutt T.R. (1988), *J. Fluid Mech.* 186, 199-222 Loth E. (2000), Progr. in Energy Combust. and Sci. 26, 161-223 Boivin M., Simonin O., Squires K.D., 1998, J. Fluid Mech. 375, pp. 235-263





Hope the memory is now refreshed....

...



# <u>Memory refreshed</u>



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- 3 How Flow Structures in Boundary Layers control Deposition/Entrainment?
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- 5 Update on Homeworks and Project.

- 1 Interpolation methods...
- \* Caveat: I will not explain them (!) I will just list some of the most employed in this business... eventually, you will know what to read/use





Momentum Equation for particle: •X(t) = Lagrangian trajectory of the particle •u(X(t),t) = particle velocity

$$\frac{d\mathbf{X}(t)}{dt} = \mathbf{u}(\mathbf{X}(t), t)$$



Schematics of Cartesian grid: P(x,y,z,t) = Instantaneous patricle position



#### Linear Interpolation



Given the fluid velocity at grid nodes,  $u(x_i, y_j, z_k, t)$ ,

the interpolated velocity value is:

$$\mathbf{u}_{\text{int}} = \sum_{i=0}^{N_x} \sum_{j=0}^{N_y} \sum_{z=0}^{N_z} \mathbf{u}(x_i, y_j, z_k, t) P_i(x) P_j(y) P_k(z)$$
(1)

where:





#### Lagrange Interpolation



Given the fluid velocity at grid nodes,  $u(x_i, y_j, z_k, t)$ , the interpolated velocity value is:

$$\mathbf{u}_{\text{int}} = \sum_{i=0}^{N_x} \sum_{j=0}^{N_y} \sum_{z=0}^{N_z} \mathbf{u}(x_i, y_j, z_k, t) L_i(x) L_j(y) L_k(z)$$
(2)

#### **Definition of Lagrange polynomials:**

$$L_{i}(x) = \frac{(x - x_{0})(x - x_{1})\dots(x - x_{i-1})(x - x_{i+1})\dots(x - x_{n-1})(x - x_{n})}{(x_{i} - x_{0})(x_{i} - x_{1})\dots(x_{i} - x_{i-1})(x_{i} - x_{i+1})\dots(x_{i} - x_{n-1})(x_{i} - x_{n})} = \sum_{j=0}^{n} \frac{x - x_{j}}{x_{i} - x_{j}}; \quad i = 0, 1, \dots, n$$

where *n* is the degree of the Polynomial.



#### Lagrange Interpolation



**n**=2: Lagrange Interpolation = Linear Interpolation!

**n=4:** 4<sup>th</sup> order Lagrange Interpolation

*n*=6: 6<sup>th</sup> order Lagrange Interpolation







#### Shape Functions Method



(3)

Given the fluid velocity at grid nodes,  $u(x_i, y_j, z_k, t)$ , the interpolated velocity value is:

$$\mathbf{u}_{\text{int}} = \sum_{i=0}^{N_x} \sum_{j=0}^{N_y} \sum_{z=0}^{N_z} \left[ \mathbf{u}(x_i, y_j, z_k, t) H_i(x) H_j(y) H_k(z) + \frac{\partial \mathbf{u}}{\partial x} (x_i, y_j, z_k, t) G_i(x) H_j(y) H_k(z) + \frac{\partial \mathbf{u}}{\partial y} (x_i, y_j, z_k, t) H_i(x) G_j(y) H_k(z) + \frac{\partial \mathbf{u}}{\partial z} (x_i, y_j, z_k, t) H_i(x) H_j(y) G_k(z) \right]$$

The method is based on using the derivatives of  $u(x_i, y_j, z_k, t)$  in the 8 nodes of the cell containing the particles together with the <u>Shape Functions</u> G and H.



# Shape Functions Method









Interpolation	Computational Co	ost	<b>Truncation Error</b> $\underline{B}$
Linear/Lagr. ord. 2	24 M		$E_t \propto O(\Delta x)^2$
Shape Function	96 M	C o	$E_t \propto O(\Delta x)^4$
Lagrangian order 4	$2 \cdot (3 \cdot 4^3 \cdot M)$	#	$E_t \propto O(\Delta x)^4$
Lagrangian order 6	$2 \cdot (3 \cdot 6^3 \cdot M)$	Ļ	$E_t \propto O(\Delta x)^6$

A For a <u>number of particles M</u>, the computational cost is given by the number of floating-point operations required to compute the triple sum in Eqs. (1), (2), (3).

<sup>B</sup> The truncation error, defined as the difference between exact and interpolated velocity values, gives an estimate of interpolation accuracy.





## Example of influence of interpolation









# Just in case books would not

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ELSEMIER	Computers & Fluids 36 (2007) 1187-1199



Simple and accurate scheme for fluid velocity interpolation for Eulerian–Lagrangian computation of dispersed flows in 3D curvilinear grids

Cristian Marchioli \*.\*. Vincenzo Armenio b. Alfredo Soldati

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•1 Interactions of Inertial Particles and Coherent Structures; >> From Microscale Interaction to Macroscale Effects.



Examples of Particle/Structure Interaction



# 1. Turbulent Boundary Layer >> Particle Trapping in the wall region.

2. Confined Jet

#### >> Selective Mechanisms for particle radial dispersion





















This is the typical result of our computational experiments!





#### **Observation** –

In Bounded flows particles accumulate at the wall at different rates depending on their inertia (forces:drag and inertia)

Accumulation at the wall is turbulence induced and non uniform. Phenomenon will persist from a qualitative viewpoint until gravity will dominate (large particles)













# What are the Low Speed Streaks? Consider an isosurface of Streamwise velocity u=0.56 Uc



Red: Low-Speed Streamwise Streaks







Observation – The same thing that generates the Low-Speed Streaks controls particle Transfer and segregation







# Conclusion – Wall structures dominate particle wall transfer fluxes

Green: CounterCLKWS Rotating Quasi Strmws Vortex (ω<sub>x</sub>)

Blue: CLKWS Rotating Quasi Strmws Vortex (ω<sub>x</sub>)

**Red:** Particles Approaching the Wall

> Pale Blue: Particles Leaving the Wall



Part III





#### Conclusion – Wall structures dominate particle wall transfer fluxes



Close up (z+ < 50) of the buffer region of the TBL.  $\tau_p^+=25$  particles under (Drag Force Only) are effectivelyTransferred by Coherent Structures

Part III



1. Turbulent Boundary Layer:

From microscale phenomena to Macroscale Effects



Snapshot of Inertial Particles and Wall Structures.1.

Back  $\Rightarrow$  to the wall Blue  $\Rightarrow$  off the wall

Circles  $\Rightarrow$  Neglig. Vel.







Snapshot of Inertial Particles and Wall Structures.2. Preceeding vortex tail forbid ejection area to some particles





# 2. Bounded Jet:

From microscale phenomena to Macroscale Effects



#### Motivation and Flow Geometry: Diesel Exhaust Filtering System





#### 2. Bounded Jet:

From microscale phenomena to Macroscale Effects



Particles undergo selective Radial Dispersion due to their different inertia













2. Bounded Jet:

From microscale phenomena to Macroscale Effects



Interaction among small particles (10  $\mu$ m ) and all flow structures characterized by vorticity modulus.





#### 2. Bounded Jet: Particle behavior





#### INNER PARTICLES

follow initially the jet core. Entrainment in the shear-layer. Large dispersion in the outer region.

#### **OUTER PARTICLES**

Follow the shear-layer foldup. After pairing, vortex dissociates into smaller structures. Annular *CLUSTERS* observed.

Larger dispersion generated by LOCALLY GENERATED TURBULENCE and NOT by upstream-generated (inlet) turbulence

# Bibliography (suggested readings)



#### **Microscale Phenomena and Macroscale Effects**

Chung, J.N. and Troutt, D.R. (1988) J. Fluid Mech., v. 186, p. 199

Marchioli, C. and Soldati, A. (2002) J. Fluid Mech., v. 468, p. 283

Eaton, J.k. and Fessler, J.R. (1994) Int. J. Multiphase Flow, v. 20, p. 169

Marchioli, C., Giusti, A., Salvetti, M.V. and Soldati, A. (2003) *Int. J. Multiphase Flow*, v. **29**, p. 1017

Sbrizzai, F., Verzicco, R., Pidria, F. and Soldati, A. (2004) Int. J. Multiphase Flow, v. **30**, p. 1389-1417

Campolo, M., Salvetti, M.V., and Soldati, A. (2005) AIChE J., v. 51, p. 28-43

Sbrizzai, F., Faraldi, P. and Soldati A. (2005), Chem. Eng. Sci., 60, p. 6551-6563

Soldati A. (2005), ZAMM , **85** , 683-699.

Picciotto, M., Mrchioli, C. and Soldati A. (2005), Phys. Fluids, 17.

#### <u>Part III</u>



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1 Measurements of particle preferential distribution; >> Examples in Archetypal Flows





# **Objectives:**

# 1. Measure non homogeneity in particle distribution

# 2. Understand non homogeneity in particle distribution

 $\rightarrow$  Identify parameters to control particle distribution...



Small-scale particle clustering (Bec et al., 2004)



# **Observation**



Particle distribution in 2-D turbulent flow is NOT homogeneous

How much?





# Ref: Grassberger & Procaccia, Physica D, 1984



The number of particles in a sphere of radius r identifies the Fractal dimension of the sub-space where particles cluster

 $N(r) \propto r_{\nu}$ 

 $\upsilon = \lim_{r \to 0} \frac{dN(r)}{dr}$ 

v = correlation dimension





### 1-D Correlation or 4-D Simulation? Example 4. Particle Laden Jet in Crossflow





- 10 micron particles
- Particles follow the coherent structures.
- Collect in the highstrain low-vorticity regions between vortices (Squires & Eaton, 1991)



# Example of particle clustering: JICF







#### Correlation dimension: JICF





# $T_{slv}$ circulation of shear layer vortices $T_{roll-up}$ formation of shear layer vortices



Particle clustering: 3. Flow topology characterization





![](_page_58_Picture_0.jpeg)

## Particles and Flow Topology.3. Wall region $(z^+ < 5)$

![](_page_58_Picture_2.jpeg)

![](_page_58_Figure_3.jpeg)

re than 70 % of particles in the convergence regions (III and IV Hard to see the regions in a 3D space...

![](_page_59_Picture_0.jpeg)

#### Particles and Flow Topology.4.

![](_page_59_Picture_2.jpeg)

#### At the wall the velocity gradient tensor degenerates: only du'/dz and dv'/dz are non zero (z+=0).

![](_page_59_Figure_4.jpeg)

![](_page_60_Picture_0.jpeg)

![](_page_60_Picture_1.jpeg)

A possibility to control wall particle distribution is to control instantaneous wall shear stress.

![](_page_60_Figure_3.jpeg)

Behavior of the spanwise strain rate component along the line A-A

**STA: Short Term Accumulation** 

**.TA: Long Term Accumulation** 

Instantaneous St=25 particle distribution in the viscous sublayer, z+5. The mean flow is

directed top down.

![](_page_61_Picture_0.jpeg)

# *is there an optimum for particle non-uniform distribution? To characterize their non-uniformity...*

![](_page_61_Picture_2.jpeg)

![](_page_61_Figure_3.jpeg)

![](_page_61_Figure_4.jpeg)

![](_page_61_Figure_5.jpeg)

![](_page_61_Figure_6.jpeg)

**D** =  $(\sigma - \sigma_p)/\lambda$ , with  $\lambda$  = average number of particle per cell

 $\sigma$  = standard deviation of the PDF

![](_page_62_Picture_0.jpeg)

![](_page_62_Figure_1.jpeg)

![](_page_63_Figure_0.jpeg)

![](_page_64_Figure_0.jpeg)

![](_page_65_Picture_0.jpeg)

### Deviation from random distribution

![](_page_65_Picture_2.jpeg)

# Bubbles

![](_page_65_Figure_4.jpeg)

# References

Grassberger & Procaccia, "Measuring the strangeness of strange attractors", *Physica D*, 9, 189, 1984

Tang, Wen, Yang, Crowe, Chung, Troutt, "Self-organizing particle dispersion mechanism in plane wake", *Phys. Fluids*, 4, 2244, 1992

Fessler, Kulick & Eaton, "Preferential concentration of heavy particles in a turbulent channel flow", *Phys. Fluids*, 6, 3742, 1994

Picciotto, Marchioli, and Soldati "Characterization of near-wall accumulation regions for inertial particles in turbulent boundary layers", *Phys. Fluids*, 17, 2005

# **Computational Fluid Dynamics database**

![](_page_67_Picture_1.jpeg)

Free CFD database, kindly hosted by Cineca supercomputing center (Bologna, Italy).

Over than 1 Tbyte DNS fluiddynamics data available on line at:

http://cfd.cineca.it/cfd